

FPN II

This is the third - 79 - section taken from

Three Analytical Studies Pertinent  
to Structural Testing  
KN-69-202 (R)

15 May 1969

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Preliminary Analysis of Heating Effects and  
Velocity Response of Magnetically Driven Plates

PRELIMINARY ANALYSIS OF HEATING EFFECTS AND  
VELOCITY RESPONSE OF MAGNETICALLY DRIVEN PLATES

**A. INTRODUCTION**

The structural testing facilities of Kaman Nuclear include three rather large scale capacitor banks which, individually, are capable of driving practical size plates by magnetically generated forces. It is currently envisioned that each of these banks may be used for an assortment of input testing techniques. In order to assure a judicious choice of experimental inputs (capacitor voltage, flyer type, initial flyer separation distance, etc.) on any particular problem, it is necessary to develop a theoretical model(s) which will be able to predict at least some of the response behavior of the capacitor-flyer system. This report describes the initial steps taken to accomplish this goal.

The mathematical procedure to be outlined in the next section will be restricted in application to flat, thin flyer plates. The thin requirement implies that gradients across the plate thickness will be ignored. Both of these restrictions are rather severe and hopefully, they will eventually be removed. At present the judgment of the accuracy of this model can only be made by comparing its conclusions (i.e., flyer velocity, flyer heating) with experiments.

In Section B, the physical problem will be translated into a mathematical framework. Section C will consist of a discussion of the numerical solution technique, a detailed listing of a related Fortran computer program, and a sample problem.

**B. DEVELOPMENT OF MAGNETIC FLYER THEORY**

This discussion is divided into two distinct phases. The first phase delineates the model for simulating the fields, currents, and forces between two current carrying parallel plates. The second phase is concerned with incorporating the parallel plate element into the capacitor bank discharge circuit, and performing a circuit response analysis.

In phase I the starting point can be a standard representation of the electromagnetic vector potential ( $\vec{A}$ ) at any field point due to a steady state current density  $\vec{J}$  at other points. This representation is

$$\vec{A} = (\mu_0/4\pi) \int_T \vec{J} \frac{d\tau}{r} \quad (1)$$

where  $\mu_0$  = permeability of free space

$T$  = volume of all space containing current

$r$  = distance from source point to field point

For a thin infinite sheet of spatially uniform current, the  $\vec{A}$  can be found rather easily. First let

$$\vec{J} = j \vec{l}_x \quad (2)$$

$\vec{l}_x$  = unit vector in x-direction

and consider the coordinate system shown in Figure 1.

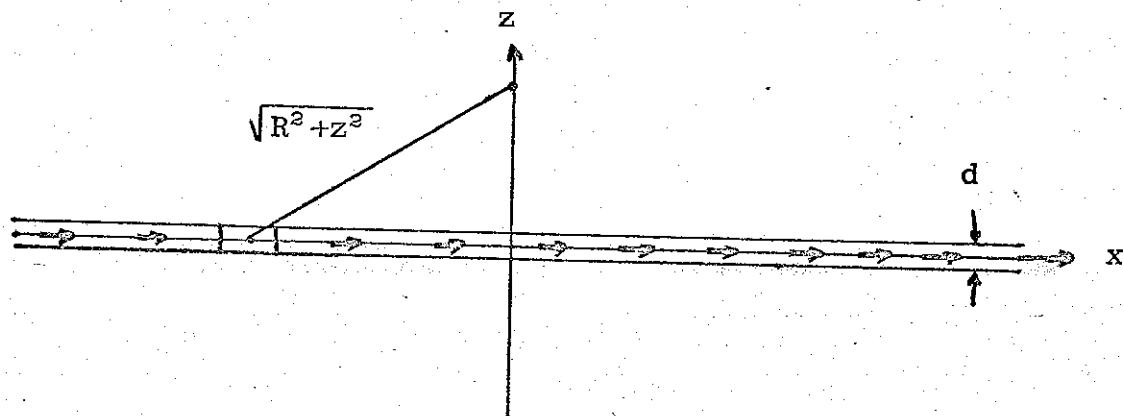


Figure 1

Integration of (1) over the current sheet can be accomplished in cylindrical coordinates. The  $\vec{A}$  field at any point on the z-axis is

$$\vec{A} = (\mu_0/4\pi) j \vec{i}_x \int_{-d/2}^{+d/2} \int_0^{2\pi} \int_0^{R_L} \frac{R dR d\theta dz}{\sqrt{R^2 + z^2}} \quad (3)$$

$$= (\mu_0 j d/2) (R_L - |z|) \vec{i}_x \quad (4)$$

where  $R_L$  is an extremely large radius.

The  $\vec{A}$  field in the neighborhood of two parallel plates can be found by superposition. Let the upper plate coincide with the plane  $z=0$  and its current density by  $j \vec{i}_x$ , and let the lower plate coincide with  $z=-D$  and its  $\vec{j} = -j \vec{i}_x$ . Then

$$\vec{A}(z) = (\mu_0 j d/2) (|z+D| - |z|) \vec{i}_x \quad (5)$$

Equation (5) implies that  $\vec{A}$  is independent of  $z$  in the volumes above both plates or below both plates. Between the plates

$$\vec{A}(z) = (\mu_0 j d) (z + D/2) \vec{i}_x \quad (6)$$

The magnetic induction vector  $\vec{B}$  and the electric field intensity  $\vec{E}$  can be found from  $\vec{A}$  by the standard relations

$$\vec{B} = \text{curl } \vec{A} \quad (7)$$

$$\vec{E} = -\frac{\partial \vec{A}}{\partial t} \quad (8)$$

Therefore, between the plates

$$\vec{B} = \vec{i}_y \frac{\partial A_x}{\partial z} = (\mu_0 j d) \vec{i}_y \quad (9)$$

$$\vec{E} = -\frac{\partial}{\partial t} ((\mu_0 j d/2) (2z + D)) \vec{i}_x \quad (10)$$

and  $\vec{E}(0)$ ,  $\vec{E}(-D)$  can be evaluated to deduce the voltage across

the plates (assuming  $\frac{dD}{dt} \ll$  speed of light)

$$\epsilon = \oint \vec{E} \cdot d\vec{l} = -\mu_0 \ell d \frac{\partial}{\partial t} (Dj) \quad (11)$$

This relationship (11) can be the voltage-current law for the parallel plate element in an external circuit when the  $j$  is replaced by the full current on the sheets (i).

$$i = bdj \quad (12)$$

b = width of sheets

$$\epsilon = -(\mu_0 \ell / b) \frac{\partial}{\partial t} (Di) \quad (13)$$

$$= -\frac{\partial}{\partial t} (L_p i) \text{ if } L_p = \mu_0 \ell D/b$$

The last step in phase I is concerned with the magnetic force exerted on one plate by its parallel counterpart. The Lorentz law can be used.

$$\vec{F} = i d\vec{l} \times \vec{B} \quad (14)$$

$\vec{F}$  = total force on plate

The  $\vec{B}$  field in (14) is the  $\vec{B}$  on one plate due to current in the other. Thus on the lower plate

$$\vec{B} (-D) = (\mu_0 j d/2) \vec{i}_y$$

$$d\vec{l} = -\vec{i}_x dx$$

and then

$$\vec{F} = -(\mu_0 \ell / 2b) i^2 \vec{i}_z \quad (15)$$

Equations (13) and (15) give the voltage across the parallel plates and the force between the plates as a function of the total current.

Phase II can now be started. Consider the circuit diagram in Figure 2.

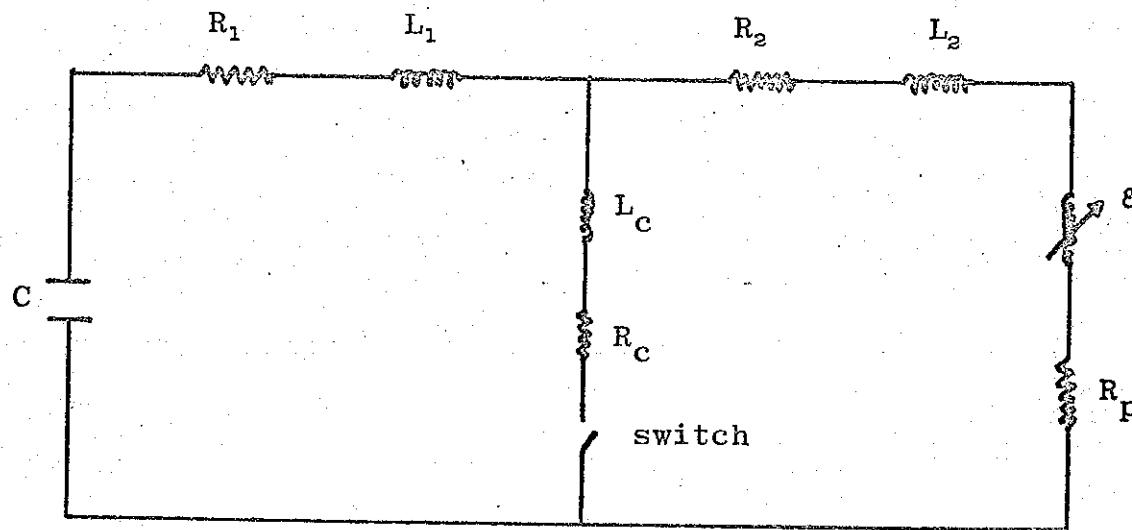


Figure 2

The subscripts on the symbols for resistance (R), inductance (L), and current i are 1 for loop 1 line quantities, 2 for loop 2, c for the L and R in the "crowbar" switch line, and p for parallel plate variables. This is a straight forward series circuit except for the crowbar line which is switched in at some specified time after the start of the capacitor discharge.

The parallel plate element has a nonlinear relationship between  $\epsilon$ , i, and D when D is allowed to vary during the course of the discharge. Thus the more simple methods of circuit analysis (i.e., Laplace transforms) are not useful, and a finite difference approach is necessary. The governing circuit equations corresponding to Figure 2 will be formulated in terms of first order derivatives in order to facilitate this finite differencing.

Before the crowbar is switched in at time  $(t) = t_s$ , the sum of the voltage around the simple circuit is zero. Mathematically this is stated by

$$q/C + (L_1 + L_2) \frac{di}{dt} + (R_1 + R_2 + R_p)i + \frac{d}{dt}(L_p i) = 0 \quad (16)$$

where

$q$  = charge on capacitor

$C$  = capacitance of bank

Equation (16) has 4 implied unknowns ( $q$ ,  $i$ ,  $D$ , and  $\frac{dD}{dt}$ ) and thus 3 more equations are necessary to start a numerical procedure. These are

$$\frac{dq}{dt} = i \quad (17)$$

$$\frac{dD}{dt} = \text{plate velocity} = v \quad (18)$$

$$\frac{dv}{dt} = \frac{\text{force on plate}}{\text{mass of plate (M)}} = \frac{\mu_o l}{2bM} i^2 \quad (19)$$

Before solution, equation (16) can be rearranged to a symmetrical form.

$$\frac{di}{dt} = -\{q/C + (R_1 + R_2 + R_p)i + (\mu_o l/b)vi\}/(L_1 + L_2 + L_p) \quad (20)$$

Since Equations (20), (21) are already nonlinear, it requires very little additional effort to allow all the resistances to vary with total heat generated in each. A way of formulating this behavior is to assume a linear dependence of resistance on

deposited energy. For example let

$$R_2 = R_{20} + g_2 E_2 \quad (21)$$

where

$$E_2 = \int_0^t i^2 R_2 dt \quad (22)$$

$g_2$  = resistance/energy coefficient

$R_{20}$  = initial resistance

The  $E_2$  is a measure of time dependent temperature of the resistor. All equations are now complete except for a listing of the initial conditions of the dependent variables. These are

$$q(0) = -Q \quad (23)$$

$$i(0) = 0 \quad (24)$$

$$v(0) = 0 \quad (25)$$

$$D(0) = D_i \quad (26)$$

Equations (17) through (20) will be finite differenced in Section C.

After the switching time ( $t_s$ ) a new set of similar equations with new initial conditions must be solved. Figure 2 shows two loop currents ( $i_1$ ,  $i_2$ ) and Kirchhoff's laws supply two loop equations. These loop equations can be written

$$\alpha_{11} \frac{di_1}{dt} + \alpha_{12} \frac{di_2}{dt} = \alpha_{13} \quad (27)$$

$$\alpha_{21} \frac{di_1}{dt} + \alpha_{22} \frac{di_2}{dt} = \alpha_{23} \quad (28)$$

with

$$\alpha_{11} = L_1 + L_C \quad \alpha_{12} = \alpha_{21} = -L_C$$

$$\alpha_{22} = L_2 + L_p + L_c$$

$$\alpha_{13} = -q/c - (R_1 + R_c)i_1 + R_c i_2$$

$$\alpha_{23} = R_c i_1 - (R_2 + R_p + R_c + \mu_o l v/b) i_2$$

The derivatives in (27) and (28) can be isolated by solving two equations and two unknowns.

$$\frac{di_2}{dt} = \frac{\alpha_{11} \alpha_{23} - \alpha_{21} \alpha_{13}}{\alpha_{11} \alpha_{22} - \alpha_{21} \alpha_{12}} \quad (29)$$

$$\frac{di_1}{dt} = \frac{\alpha_{13}}{\alpha_{11}} - \frac{\alpha_{12}}{\alpha_{11}} \left( \frac{\alpha_{11} \alpha_{23} - \alpha_{21} \alpha_{13}}{\alpha_{11} \alpha_{22} - \alpha_{21} \alpha_{12}} \right) \quad (30)$$

and the other 3 equations are similarly

$$\frac{dq}{dt} = i_1 \quad (31)$$

$$\frac{dv}{dt} = (\mu_o l / 2bm) i_2^2 \quad (32)$$

$$\frac{dD}{dt} = v \quad (33)$$

Initial conditions for this problem are

$$i_1(t_s) = i_2(t_s) = i(t_s)$$

$q(t)$ ,  $v(t)$  and  $D(t)$  continue from previous values.

Thus, the governing circuit equations are specified and available for numerical solution.

### C. NUMERICAL ANALYSIS

The sets of coupled ordinary differential equations (17) through (20) and (29) through (33) can be solved by a rather simple procedure. First derivatives occurring on the left side of these equations can be replaced by finite difference approximations. As an example consider equation (17).

$$\frac{dq}{dt} = i(t)$$

$$\frac{\Delta q}{\Delta t} \approx i(t)$$

and

$$q_{\text{new}} = q_{\text{old}} + \Delta t \cdot L_{\text{old}}(t) \quad (34)$$

A "new"  $q$  can be found from an "old"  $q$  and  $i$ . Equations (18) through (20) similarly provide "new"  $D$ ,  $v$ , and  $i$  from "old" values. Thus, if initial values of  $q$ ,  $D$ ,  $v$  and  $i$  are specified, the finite difference equations such as (34) lead to a net of dependent variable values at fixed increments of time. Obviously a smaller values of  $\Delta t$  corresponds to smaller errors in advanced time quantities. The actual size of  $\Delta t$ , however, can be adjusted by trial and error until the energy for the system is "properly" conserved (to enough significant figures).

The Fortran program which performs this analysis and assists in plotting various output quantities is called MAGFL. To assist

the interested reader in deciphering this program a dictionary of variables is listed below.

AN, NAA	= number of problems
VC	= initial capacitor voltage
C	= bank capacitance
R10, R20, RP0, RCO	= initial resistance of $R_1$ , $R_2$ , $R_p$ , $R_c$
G1, G2, GP, GC	= $g_1$ , $g_2$ , $g_p$ , $g_c$ resistance/energy coefficient
AL1, AL2, ALC	= $L_1$ , $L_2$ , $L_c$ inductance values
ALENG	= plate length
B	= plate width
AMASS	= plate mass
D0	= initial plate separation distance
TP	= maximum time in problem
TS	= crowbar switching time
DTC	= zoning parameter
AMU	= $\mu_o$
ANP	= number of print outputs
DMAX	= maximum allowable displacement
WO	= initial angular frequency
DT	= time increment
ANC	= number cycles in problem
ANCPP, NCPP	= number of cycles per printout
T	= time

Q0	= initial capacitor charge
E1, E2, EP, EC	= total energy deposited in 4 resistors
QØ, DØ, VØ, AIØ	= "old" q, D, v, i
QN, DN, VN, AIN	= "new" q, D, v, i
ALP	= current inductance of plates
EOTH	= energy sum parameter
R1, R2, RP, RC	= instantaneous resistances
IFLAG	= 1 after $t=t_s$
TT (M)	= time vector used in plotting subroutine
VOLT (M)	= capacitor voltage
PE (M)	= percent of initial energy in kinetic energy of flyer
D (M)	= displacement
V (M)	= flyer velocity
EPM (M)	= heat deposited in parallel plates
RPM (M)	= resistance of plates
EBAL (M)	= 1.000 for appropriate zoning
SI (M)	= top level of flyer

After the listing of MAGFL in the following pages a sample problem will be introduced.

```
PROGRAM MAGFL(INPUT,OUTPUT)
DIMENSION TT(100),VOLT(100),D(100),V(100),AI(100),EPM(100),RPM(100),
1,EOM(100),PE(100),EBAL(100),TIT1(4),TIT2(3),TIT3(3),SI(100),
2TIT4(3),TIT5(4),TIT6(5),TIT7(5)
DATA (TIT1(1)=8HCAPACITO),(TIT1(2)=8HR VOLTAG),(TIT1(3)=8HE VS TIME
1),(TIT1(4)=8HE )
DATA (TIT2(1)=8HFLYER CU),(TIT2(2)=8HRRENT VS),(TIT2(3)=8H TIME
1)
DATA (TIT3(1)=8HEFFICIEN),(TIT3(2)=8HCY VS TI),(TIT3(3)=8HME
1)
DATA (TIT4(1)=8HFLYER VE),(TIT4(2)=8HLOCITY V),(TIT4(3)=8HS TIME
1)
DATA(TIT5(1)=8HFLYER VE),(TIT5(2)=8HLOCITY V),(TIT5(3)=8HS DISTAN
1),(TIT5(4)=8HCE )
DATA (TIT6(1)=8HDISTANCE),(TIT6(2)=8H VS TIME)
DATA (TIT7(1)=8HD-IN MIL),(TIT7(2)=8HS VS TIME),(TIT7(3)=8HE
1)
READ 1000,AN
NAA=AN
DO 999 KK=1,NAA
C      READ CIRCUIT CHACTERISTICS
READ 1000,VC,C,R10,G1,AL1,R20,G2,AL2
READ 1000,RC0,GC,ALC
READ 1000,ALENG,B,AMASS,RP0,GP,D0
READ 1000,TP,TS
AMU=.00000126
DTC=.001
ANP=99.
DMAX=5.
PRINT 2000
PRINT 2010,R10,AL1,R20,AL2
PRINT 2020,G1,G2
PRINT 2030
PRINT 2040
PRINT 2040 $ PRINT 2040
PRINT 2050
PRINT 2060,RC0
PRINT 2070,GC,RP0
PRINT 2080,GP
PRINT 2090 $ PRINT 2090
PRINT 2100
PRINT 2110,VC
PRINT 2120
PRINT 2130,ALC
PRINT 2140,D0
PRINT 2150,C,B
PRINT 2160,ALENG
PRINT 2170,AMASS
PRINT 2040
PRINT 2180
PRINT 2190,TS
PRINT 2040 SPRINT 2040 $ PRINT 2040 $ PRINT 2040
PRINT 2200
PRINT 2210
AL=AL1+AL2+AMU*D0*ALENG/B
W0=(AL*C)**(-.5)
DT=DTC/W0
```

```
ANC=TP/DT
ANCPP=ANC/ANP
NCPP=ANCPP
IF(NCPP.LT.10) NCPP=10
PRINT 1050,TP,DT,NCPP
T=0.
J=0
P1=AMU*ALENG/(B*AMASS)
P2=P1*AMASS
Q0=-C*VC
Q0=Q0
E1=0.
E2=0.
EP=0. $EC=0.
DO=DO
M=1
AIO=0.
VO=0.
DN=0.
R2=R20
R1=R10
RC=RC0 $RP=RP0 $IFLAG=0
100 IF(T.GT.TP) GO TO 600
IF(T.GT.TS) GO TO 300
IF(DN.GT.DMAX) GO TO 600
QN=Q0+AIO*DT
DN=DO+VO*DT
VN=VO+P1*(AIO**2)*DT /2.
E2=E2+(AIO**2)*R2*DT
E1=E1+(AIO**2)*R1*DT
EP=EP+(AIO**2)*RP*DT
R2=R20+G2*E2
R1=R10+G1*E1
RP=RP0+GP*EP
ALP=AMU*ALENG*DO/B
AIN=AIO-DT*(Q0/C+(R1+R2+RP)*AIO+P2*VO*AIO)/(AL1+AL2+ALP)
EOTH=.5*(AL1+AL2+AMU*ALENG*DN/B)*(AIN**2)+.5*(QN**2)/C
T=T+DT
Q0=QN
DO=DN
VO=VN
AIO=AIN
J=J+1
IF(J.EQ.NCPP) GO TO 500
GO TO 100
300 AILO=AIO
AIRO=AIO
A11=A11+ALC
A21=-ALC
A12=-ALC
320 IF(T.GT.TP) GO TO 600
QN=Q0+DT*AILO
DN=DO+VO*DT
VN=VO+DT*P1*(AIRO**2)/2.
E1=E1+(AILO**2)*R1*DT
E2=E2+(AIRO**2)*R2*DT
EP=EP+(AIRO**2)*RP*DT
EC=EC+((AIRO-AILO)**2)*RC*DT
```

```
R1=R10+G1*E1
R2=R20+G2*E2
RP=RP0+GP*EP
RC=RC0+GC*EC
A13=-Q0/C-(R1+RC)*AILO+RC*AIRO
A23= RC*AILO-(R2+RP+RC+AMU*ALENG*VO/B)*AIRO
A22=ALC+AL2+P2*D0
BB=(A11*A23-A21*A13)/(A11*A22-A21*A12)
AIRN=AIRO+DT+BB
AILN=AILO+DT*(A13/A11-(A12/A11)*BB)
EOTH=.5*(AL1)*(AILN**2)+.5*(AL2+P2*DN)*(AIRN**2)+.5*(ALC)*((AIRN
1-AILN)**2)+.5*(QN**2)/C
T=T+DT
Q0=QN
D0=DN
V0=VN
AILO=AILN
AIRO=AIRN
J=J+1
IFLAG=1
IF(J.EQ.NCPP) GO TO 500
GO TO 320
500 TT(M)=T
VOLT(M)=-QN/C
PE(M)=C*AMASS*(VN**2)/(Q0**2)
D(M)=DN
V(M)=VN
EPM(M)=EP
RPM(M)=RP
EOM(M)=EOTH
EBAL(M)=C*(EOTH+E1+E2+EP+EC+.5*AMASS*(VN**2))/(.5*(Q0**2))
SI(M)=AMASS*VN/(B*ALENG)
IF(IFLAG.EQ.1) GO TO 550
AI(M)=AIN
M=M+1 $J=0 $GO TO 100
550 AI(M)=AIRN
M=M+1
J=0
GO TO 320
600 MMAX=M-1
PRINT 1005
PRINT 1060
PRINT 1070
PRINT 1075
DO 700 M=1,MMAX
D(M)=D(M)*100.
V(M)=.0001*V(M)
TT(M)=1000000.*TT(M)
SI(M)=10.*SI(M)
IF(M.NE.50) GO TO 680
PRINT 1005 $PRINT 1060$ PRINT 1070$ PRINT 1075
680 PRINT 1080,TT(M),VOLT(M),AI(M),RPM(M),EPM(M),EOM(M),PE(M),EBAL(M),
ID(M),V(M),SI(M)
700 CONTINUE
CALL PLOT CT1(TT,VOLT,MMAX,10.,8.,1H*,TIT1,4)
CALL PLOT CT1(TT,AI,MMAX,10.,8.,1H*,TIT2,3)
CALL PLOT CT1(TT,PE,MMAX,10.,8.,1H*,TIT3,3)
CALL PLOT CT1(TT,V,MMAX,10.,8.,1H*,TIT4,3)
```

```
CALL PLOT CT1(D,V,MMAX,10..8.,1HM,TIT5,4)
CALL PLOT CT1(TT,D,MMAX,10.,R,1HM,TIT6,2)
DO 720 M=1,MMAX
720 D(M)=D(M)/(.00254)
CALL PLOT CT1(TT,D,MMAX,10.,R,1HM,TIT7,3)
999 CONTINUE
STOP
1000 FORMAT(8E10.3)
1005 FORMAT(///*1*)
1050 FORMAT(*      TIME MONITORED UNTIL =*,E10.3,* WITH INCREMENT=*,E10
1.3,* SEC   NUMBER OF CYCLES PER PLOT =*,I5//)
1060 FORMAT(8X,      *TIME      VOLTAGE      CURRENT      FLYER      HEAT IN
1  STORED      EFFICIENCY      ENERGY      PLATE      PLATE      SPECIFI
2C*)
1070 FORMAT(19X,*ON CAP      IN FLYER      RESISTANCE      FLYER      LC ENERGY 0
1F SYSTEM      BALANCE      SEPARATION      VELOCITY      IMPULSE*)
1075 FORMAT(7X,* (USEC)      (VOLTS)      (AMPS)      (OHMS)      (JOULES)
1(JOULES)*,26X,* (CM)      (CM/USEC)      (TAPS)*/)
1080 FORMAT(5X,11E11.2)
2000 FORMAT(*1*,38X,*CIRCUIT DIAGRAM*///)
2010 FORMAT(12X,*R10=*,E10.3,*    L1=*,E10.3,*    R20=*,E10.3,*    L2=*,E
1E10.3)
2020 FORMAT(13X,*G1=*,E10.3,22X,*G2=*,E10.3,/ )
2030 FORMAT(9X,*----RRRR----LLL-----RRRR----LLL
1-----*)
2040 FORMAT(9X,*--*,30X,*--*,30X,*--*)
2050 FORMAT(9X,*--*,30X,*R*,30X,*--*)
2060 FORMAT(9X,*--*,30X,*R      RCROWBAR=*,E10.3,RX,*--*)
2070 FORMAT(9X,*--*,30X,*R      GCBAR=*,E10.3,RX,*R      RPLATES=*,E10.3)
2080 FORMAT(9X,*--*,30X,*R*,30X,*R      GPLATE=*,E10.3)
2090 FORMAT(9X,*--*,30X,*--*,30X,*R*)
2100 FORMAT(9X,*-- INITIAL CAPACITOR=*,10X,*--*,30X,*--*)
2110 FORMAT(9X,*-- VOLTAGE =*,E10.3,7X,*--*,30X,*--*)
2120 FORMAT(8X,*CCC*,29X,*--*,30X,*--*)
2130 FORMAT(8X,*CCC*,29X,*L      LCROWBAR=*,E10.3,RX,*--*)
2140 FORMAT(9X,*--*,30X,*L*,30X,*E      D(0)=*,E10.3)
2150 FORMAT(9X,*-- CAPACITANCE=*,E10.3,5X,*L*,30X,*E      WIDTH=*,E10.3)
2160 FORMAT(9X,*--*,30X,*L*,30X,*E      LENGTH=*,E10.3)
2170 FORMAT(9X,*--*,30X,*--*,30X,*E      MASS=*,E10.3)
2180 FORMAT(9X,*--*,35X,*SWITCHING TIME*,12X,*--*)
2190 FORMAT(9X,*--*,31X,*/      =*,E10.3,13X,*--*)
2200 FORMAT(9X,*-----
1-----*///)
2210 FORMAT(18X,*ALL UNITS OF THE ABOVE INPUT NUMBERS ARE CONSISTENT MK
1S*)
END
```

```
SUBROUTINE PLOT CT1 (X,Y,NX,XLN,YLN,ISYM,TITLE,NT)
DIMENSION X(1),Y(1),TITLE(1),IPLT(121),XAXIS(13)
DATA (ISPC=1H),(IPER=1H),(IPLS=1H+)
INTEGER YAXIS
C
NS=XLN
NS1=NS*10+1
NS2=NS+1
N=(YLN*6+)/4.
NY=N*4+1
ZN=N
CALL SCALE(X,NX,XLN,XMN,XSCALE)
CALL SCALE(Y,NX,ZN,YMN,YSCALE)
C
C      TITLE THE PLOT
C
IF(NT.GT.0) GO TO 30
PRINT 1030
GO TO 40
30 PRINT 1030,(TITLE(I),I=1,NT)
40 PRINT 1040.
C
C      PRINT THE PLOT ONE ROW AT A TIME
C
DO 200 I=1,NY
DO 100 J=2,NS1
100 IPLT(J) = ISPC
IPLT(1) = IPER
IPLT(NS1) = IPER
YAXIS = ISPC
J=(I-1)/4
IF(J*4.NE.I-1) GO TO 150
IPLT(1) = IPLT(NS1) = IPLS
IF(I.NE.1.AND.I.NE.NY) GO TO 120
DO 110 L=1,NS1
IPLT(L) = IPER
IF((L-1)/10*10.EQ.L-1) IPLT(L)=IPLS
110 CONTINUE
120 AL=(N-J)*YSCALE+YMN
ENCODE(9,1000,YAXIS) AL
C
C      CALCULATE THE PLOT POSITIONS
C
150 DO 180 K=1,NX
YPOINT=(Y(K)-YMN)/YSCALE
IY=YPOINT*4.+5
IY=NY-IY
IF(IY.NE.I) GO TO 180
IX = (X(K)-XMN)/XSCALE*10.+1.5
IF(IX.GT.NS1) IX=NS1
IPLT(IX) = ISYM
180 CONTINUE
PRINT 1010,YAXIS,(IPLT(J),J=1,NS1)
200 CONTINUE
IFACT=ALOG10(10.*XSCALE+XMN)
DO 250 I=1,NS2
R=I-1
```

```
1 250 XAXIS(I)=(B*XSCALE+XMN)/(10.*IFACT)
1 PRINT 1020,(XAXIS(J),J=1,NS2)
1 IF(IFACT.NE.0) PRINT 1050,IFACT
1 RETURN
1 1000 FORMAT(E9.2)
1 1010 FORMAT(X,A9,X,121A1)
1 1020 FORMAT(/2X 13F10.4)
1 1030 FORMAT(2H1 ,10A8)
1 1040 FORMAT(1H )
1 1050 FORMAT(/45X 8HX 10 ** I3)
1 END
```

SUBROUTINE SCALE(X,NX,S,XMIN,DX)

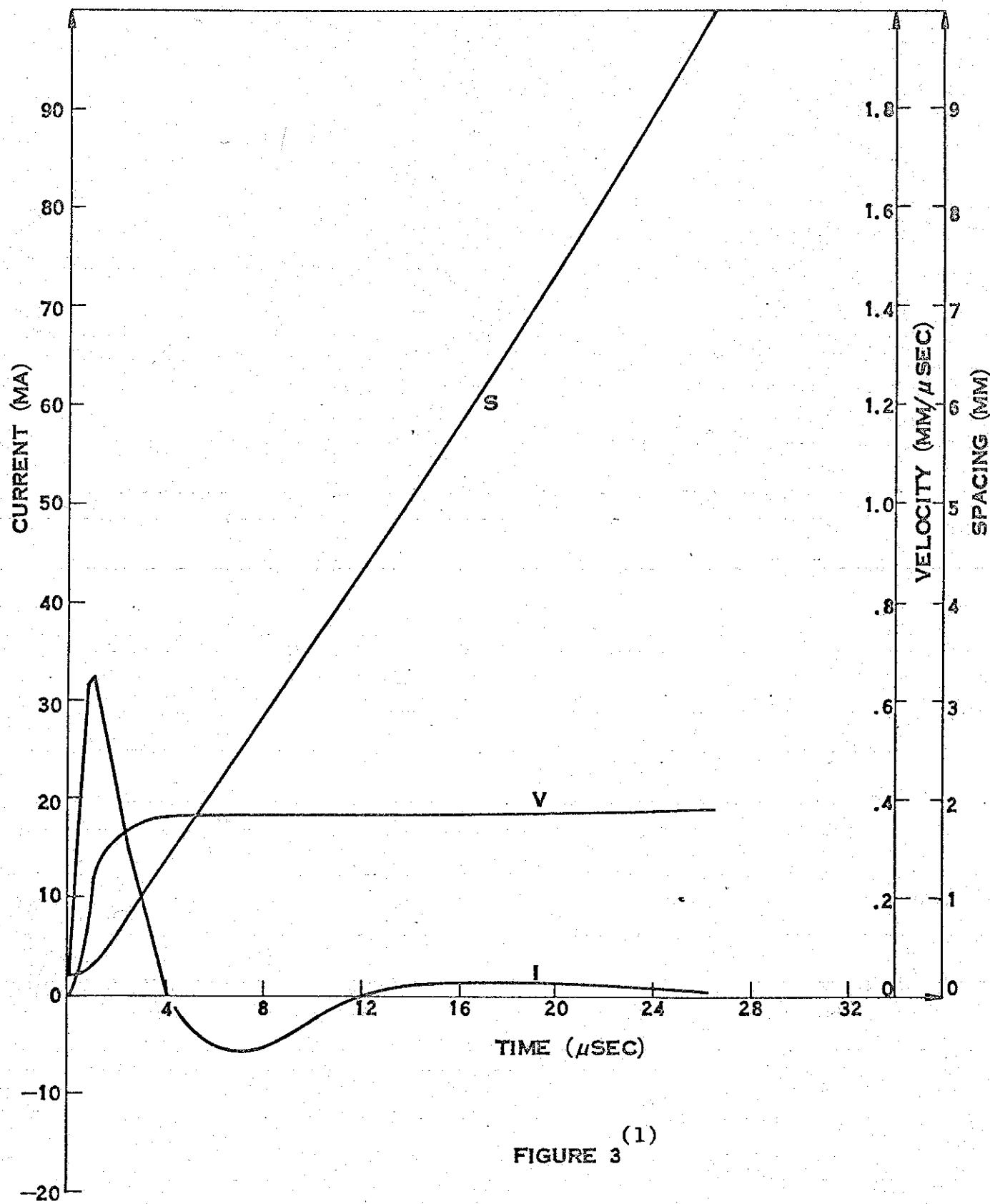
C  
C THIS SUBROUTINE FINDS MAXIMUM AND MINIMUM VALUE IN THE  
C ARRAY X. IT THEN ADJUSTS THESE TO OPTIMIZE THE PLOT WHILE  
C MAINTAINING REASONABLE VALUES FOR AXIS ANNOTATION.  
C  
C ARGUMENTS  
C X - ARRAY TO BE SCALED FOR PLOTTING.  
C N - NUMBER OF POINTS IN ARRAY X  
C S - LENGTH OF THE AXIS OVER WHICH THESE NUMBERS ARE  
C TO BE APPLIED.  
C XMIN - MINIMUM VALUE OF X  
C DX - INCREMENT OF VARIABLE FOR ONE INCH TICK ALONG AXIS  
C  
DIMENSION X(1),DXX(7)  
DATA (DXX=1.,2.,2.5,4.,5.,10.,20.)  
C DETERMINE MAXIMUM AND MINIMUM VALUES OF X  
XL = X  
XS = X  
DO 10 I=1,NX  
IF(XL.LT.X(I)) XL=X(I)  
IF(XS.GT.X(I)) XS=X(I)  
10 CONTINUE  
DS=(XL-XS)/S  
IF(DS.GT.0.) GO TO 20  
PRINT 100,(X(I),I=1,NX)  
STOP  
C DETERMINE VARIABLE INCREMENT.  
20 N=0  
ND=-1  
IF(DS.LT.1.) ND=1  
30 IF(DS.GE.1..AND.DS.LT.10.) GO TO 40  
N=N+ND  
DS=DS\*10.\*\*ND  
GO TO 30  
40 L=0  
50 L=L+1  
DX=DXX(L)  
IF(DS.GT.DX) GO TO 50  
DX=DX/10.\*\*N  
IX=XS/DX  
IF(XS.LT.0. .AND. XS.NE.IX\*DX) IX = IX-1  
XMIN=IX\*DX  
IF(XMIN+S\*DX.LT.XL\*.99999) GO TO 50  
RETURN  
100 FORMAT(1H1,\*ERROR IN INPUT ARRAY TO SCALE\*/(1H ,E18.10))  
END

The sample problem is a very simple example which has previously been solved on an analog computer at Sandia Laboratories. The analog simulation considered only a simple series circuit with an effective line resistance, a capacitor, and a resistance less parallel plate flyer. Input numbers for this problem on MAGFL are

where all units are in MKS and all formats 8E10.3.

The output of MAGFL for this problem consists of 9 pages. On the first page appears a circuit diagram with all appropriate input parameters. The second and third pages consist of a table of various dependent variables for 100 different times. (The units are reported above the columns). The next six pages plot several combinations of these quantities that are listed in the tabular output.

Figure 3 is a reproduction of the analog computer output. However, this comparison cannot be construed to be a complete check of MAGFL due to the simplified nature of the check problem.



(1)  
FIGURE 3

SANDIA LABORATORIES

1. SC-TM-69-106, "Analog Simulation of a Capacitor Bank Powered Flyer Plate", February 1969, Sandia Laboratories, Albuquerque, N. M.

CIRCUIT DIAGRAM

R10= 4.000E-04 L1= 0.

G1= 0.

R20= 0.  
G2= 0.

RRRR-----LLLL-----

R PCROWBAR= 0.  
R GCBAR = 0.  
R RPLATES= 0.  
R GPLATE= 0.

INITIAL CAPACITOR  
VOLTAGE = 4.000E+04

CAPACITANCE= 1.250E-03

CCC  
CCC

D(0)= 2.500E-04  
WIDTH= 8.000E-01  
LENGTH= 1.270E+00  
MASS= 4.480E+00

SWITCHING TIME  
= 1.000E-05

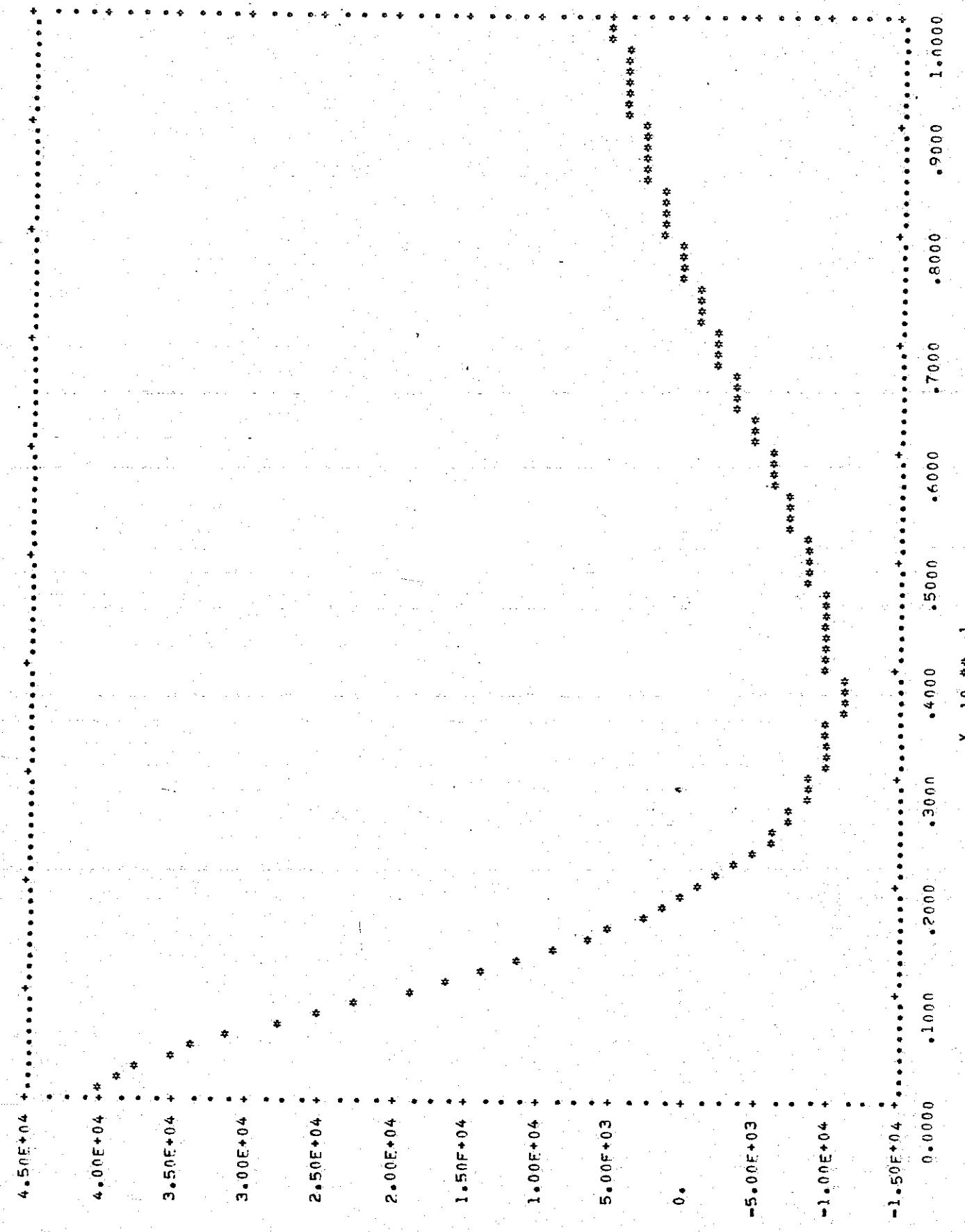
- 100 -

ALL UNITS OF THE ABOVE INPUT NUMBERS ARE CONSISTENT MKS  
TIME MONITORED UNTIL = 1.000E-05 WITH INCREMENT= 7.906E-10 SEC NUMBER OF CYCLES PER PLOT = 127

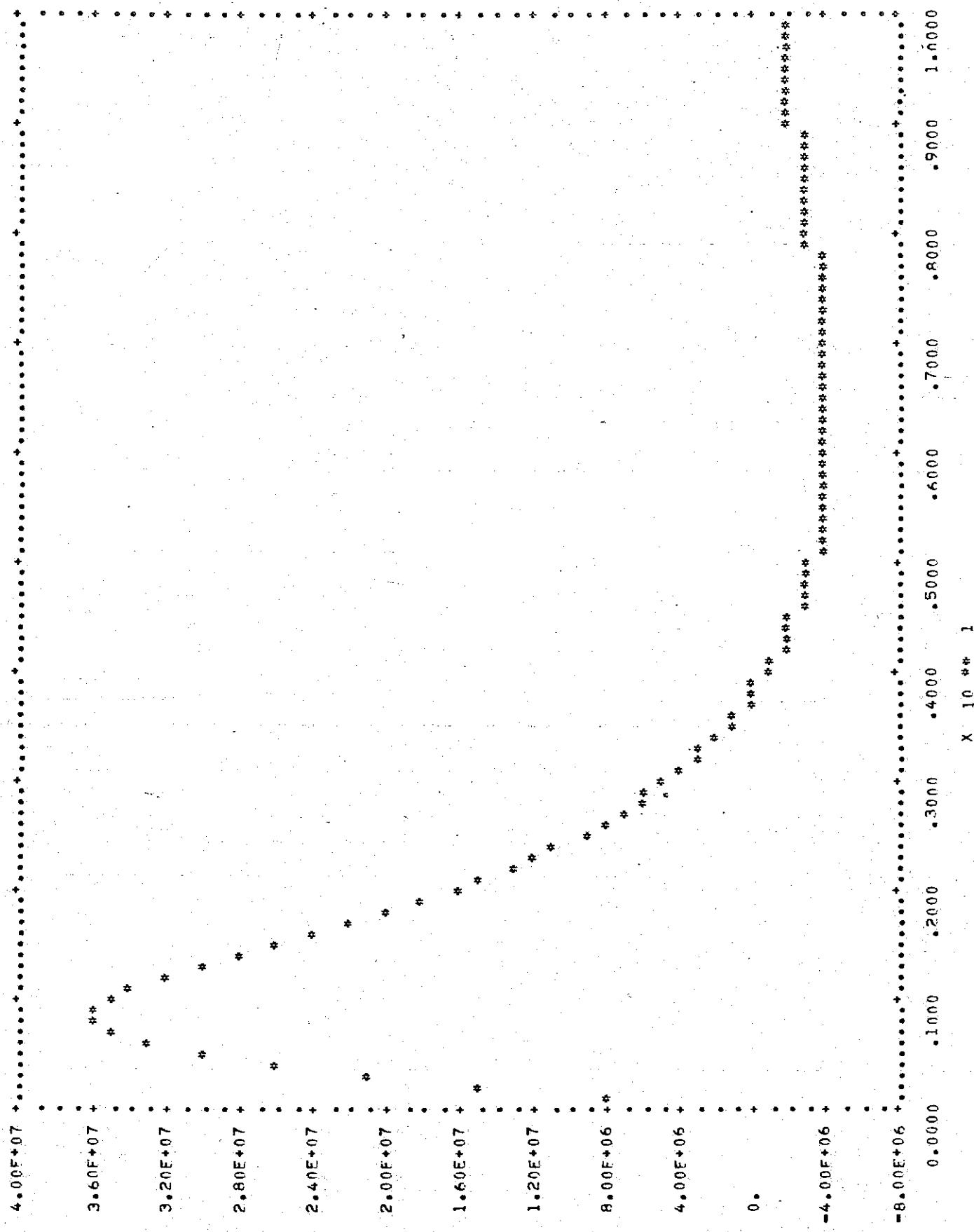
TIME (USEC)	VOLTAGE ON CAP (VOLTS)	CURRENT IN FLYER (AMPS)	FLYER RESISTANCE (OHMS)	HEAT IN FLYER (JOULES)	STORED LC ENERGY (JOULES)	EFFICIENCY OF SYSTEM	ENERGY BALANCE	PLATE SEPARATION (CM)	PLATE VELOCITY (CM/USEC)	SPECIFIC IMPULSE (TAPS)
1.00E-01	3.97E+04	7.70E+06	0.	0.	9.99E+05	4.49E-07	1.00E+00	4.48E-02	1.97E+01	1.97E-05
2.01E-01	3.88E+04	1.47E+07	0.	0.	9.94E+05	2.53E-05	1.00E+00	2.50E-02	3.36E-04	1.48E+02
3.01E-01	3.74E+04	2.08E+07	0.	0.	9.81E+05	2.49E-04	1.00E+00	2.51E-02	4.65E+02	1.05E-03
4.02E-01	3.55E+04	2.61E+07	0.	0.	9.58E+05	1.18E-03	1.00E+00	2.52E-02	2.30E-03	1.01E+03
5.02E-01	3.32E+04	3.03E+07	0.	0.	9.23E+05	3.75E-03	1.00E+00	2.56E-02	4.09E-03	1.81E+03
6.02E-01	3.06E+04	3.34E+07	0.	0.	8.77E+05	9.12E-03	1.00E+00	2.61E-02	6.38E-03	2.81E+03
7.03E-01	2.79E+04	3.53E+07	0.	0.	8.20E+05	1.83E-02	1.00E+00	2.69E-02	9.04E-03	3.99E+03
8.03E-01	2.50E+04	3.62E+07	0.	0.	7.55E+05	3.18E-02	1.00E+00	2.79E-02	1.19E-02	5.25E+03
9.04E-01	2.21E+04	3.61E+07	0.	0.	6.85E+05	4.94E-02	1.00E+00	2.92E-02	1.49E-02	6.55E+03
1.00E+00	1.92E+04	3.52E+07	0.	0.	6.13E+05	7.02E-02	1.00E+00	3.09E-02	1.77E-02	7.81E+03
1.10E+00	1.64E+04	3.38E+07	0.	0.	5.43E+05	9.30E-02	1.00E+00	3.28E-02	2.04E-02	8.99E+03
1.20E+00	1.38E+04	3.19E+07	0.	0.	4.76E+05	1.16E-01	1.00E+00	3.50E-02	2.28E-02	1.01E+04
1.31E+00	1.13E+04	2.99E+07	0.	0.	4.14E+05	1.39E-01	1.00E+00	3.74E-02	2.49E-02	1.10E+04
1.41E+00	9.00E+03	2.78E+07	0.	0.	3.59E+05	1.61E-01	1.00E+00	4.00E-02	2.68E-02	1.18E+04
1.51E+00	6.85E+03	2.57E+07	0.	0.	3.11E+05	1.81E-01	1.00E+00	4.27E-02	2.84E-02	1.25E+04
1.61E+00	4.87E+03	2.36E+07	0.	0.	2.69E+05	1.99E-01	1.00E+00	4.57E-02	2.98E-02	1.31E+04
1.71E+00	3.66E+03	2.16E+07	0.	0.	2.33E+05	2.14E-01	1.00E+00	4.87E-02	3.09E-02	1.36E+04
1.81E+00	1.40E+03	1.97E+07	0.	0.	2.02E+05	2.28E-01	1.00E+00	5.19E-02	3.19E-02	1.41E+04
1.91E+00	-1.08E+02	1.79E+07	0.	0.	1.77E+05	2.39E-01	1.00E+00	5.51E-02	3.27E-02	1.44E+04
2.01E+00	-1.48E+03	1.62E+07	0.	0.	1.55E+05	2.49E-01	1.00E+00	5.84E-02	3.33E-02	1.47E+04
2.11E+00	-2.72E+03	1.47E+07	0.	0.	1.38E+05	2.57E-01	1.00E+00	6.18E-02	3.39E-02	1.49E+04
2.21E+00	-3.84E+03	1.32E+07	0.	0.	1.23E+05	2.63E-01	1.00E+00	6.52E-02	3.43E-02	1.51E+04
2.31E+00	-4.85E+03	1.19E+07	0.	0.	1.11E+05	2.69E-01	1.00E+00	6.87E-02	3.46E-02	1.53E+04
2.41E+00	-5.75E+03	1.06E+07	0.	0.	1.02E+05	2.73E-01	1.00E+00	7.22E-02	3.49E-02	1.54E+04
2.51E+00	-6.55E+03	9.44E+06	0.	0.	9.43E+04	2.77E-01	1.00E+00	7.57E-02	3.52E-02	1.55E+04
2.61E+00	-7.27E+03	8.35E+06	0.	0.	8.83E+04	2.80E-01	1.00E+00	7.92E-02	3.53E-02	1.56E+04
2.71E+00	-7.90E+03	7.34E+06	0.	0.	8.36E+04	2.82E-01	1.00E+00	8.28E-02	3.55E-02	1.56E+04
2.81E+00	-8.45E+03	6.41E+06	0.	0.	8.01E+04	2.84E-01	1.00E+00	8.63E-02	3.56E-02	1.57E+04
2.91E+00	-8.93E+03	5.53E+06	0.	0.	7.73E+04	2.85E-01	1.00E+00	8.99E-02	3.57E-02	1.57E+04
3.01E+00	-9.34E+03	4.72E+06	0.	0.	7.54E+04	2.86E-01	1.00E+00	9.35E-02	3.57E-02	1.57E+04
3.11E+00	-9.69E+03	3.96E+06	0.	0.	7.39E+04	2.86E-01	1.00E+00	9.71E-02	3.58E-02	1.58E+04
3.21E+00	-9.98E+03	3.26E+06	0.	0.	7.29E+04	2.87E-01	1.00E+00	1.01E-01	3.58E-02	1.58E+04
3.31E+00	-1.02E+04	2.60E+06	0.	0.	7.23E+04	2.87E-01	1.00E+00	1.04E-01	3.58E-02	1.58E+04
3.41E+00	-1.04E+04	1.99E+06	0.	0.	7.19E+04	2.87E-01	1.00E+00	1.08E-01	3.58E-02	1.58E+04
3.51E+00	-1.05E+04	1.43E+06	0.	0.	7.16E+04	2.87E-01	1.00E+00	1.12E-01	3.58E-02	1.58E+04
3.61E+00	-1.06E+04	9.01E+05	0.	0.	7.15E+04	2.88E-01	1.00E+00	1.15E-01	3.58E-02	1.58E+04
3.72E+00	-1.07E+04	4.11E+05	0.	0.	7.15E+04	2.88E-01	1.00E+00	1.19E-01	3.58E-02	1.58E+04
3.82E+00	-1.07E+04	-4.30E+04	0.	0.	7.15E+04	2.88E-01	1.00E+00	1.22E-01	3.58E-02	1.58E+04
3.92E+00	-1.07E+04	-4.64E+05	0.	0.	7.16E+04	2.88E-01	1.00E+00	1.26E-01	3.58E-02	1.58E+04
4.02E+00	-1.06E+04	-8.54E+05	0.	0.	7.15E+04	2.88E-01	1.00E+00	1.29E-01	3.58E-02	1.58E+04
4.12E+00	-1.05E+04	-1.21E+06	0.	0.	7.14E+04	2.88E-01	1.00E+00	1.33E-01	3.58E-02	1.58E+04
4.22E+00	-1.04E+04	-1.55E+06	0.	0.	7.13E+04	2.88E-01	1.00E+00	1.37E-01	3.58E-02	1.58E+04
4.32E+00	-1.03E+04	-1.85E+06	0.	0.	7.10E+04	2.88E-01	1.00E+00	1.40E-01	3.58E-02	1.58E+04
4.42E+00	-1.01E+04	-2.14E+06	0.	0.	7.07E+04	2.88E-01	1.00E+00	1.44E-01	3.59E-02	1.58E+04
4.52E+00	-9.95E+03	-2.40E+06	0.	0.	7.03E+04	2.88E-01	1.00E+00	1.47E-01	3.59E-02	1.58E+04
4.62E+00	-9.75E+03	-2.63E+06	0.	0.	6.99E+04	2.88E-01	1.00E+00	1.51E-01	3.59E-02	1.58E+04
4.72E+00	-9.53E+03	-2.85E+06	0.	0.	6.93E+04	2.89E-01	1.00E+00	1.55E-01	3.59E-02	1.58E+04
4.82E+00	-9.29E+03	-3.04E+06	0.	0.	6.86E+04	2.89E-01	1.00E+00	1.58E-01	3.59E-02	1.58E+04
4.92E+00	-9.04E+03	-3.22E+06	0.	0.	6.79E+04	2.89E-01	1.00E+00	1.62E-01	3.59E-02	1.58E+04

TIME (USEC)	VOLTAGE ON CAP. (VOLTS)	CURRENT IN FLYER (AMPS)	HEAT IN FLYER (JOULES)	FLYER RESISTANCE (OHMS)	STORED LC ENERGY (JOULES)	EFFICIENCY OF SYSTEM	PLATE SEPARATION (CM)	PLATE VELOCITY (CM/USEC)	SPECIFIC IMPULSE (TAPS)
5.02E+00	-8.77E+03	-3.38E+06	0.	1.00E+00	1.65E-01	1.65E+04	3.60E-02	1.59E+04	
5.12E+00	-8.50E+03	-3.53E+06	0.	1.00E+00	1.69E-01	1.59E+04	3.60E-02	1.59E+04	
5.22E+00	-8.21E+03	-3.65E+06	0.	1.00E+00	1.73E-01	1.59E+04	3.60E-02	1.59E+04	
5.32E+00	-7.91E+03	-3.77E+06	0.	1.00E+00	1.76E-01	1.59E+04	3.60E-02	1.59E+04	
5.42E+00	-7.60E+03	-3.88E+06	0.	1.00E+00	1.80E-01	1.59E+04	3.60E-02	1.59E+04	
5.52E+00	-7.29E+03	-3.95E+06	0.	1.00E+00	1.84E-01	1.59E+04	3.61E-02	1.59E+04	
5.62E+00	-6.97E+03	-4.02E+06	0.	1.00E+00	1.87E-01	1.59E+04	3.61E-02	1.59E+04	
5.72E+00	-6.64E+03	-4.08E+06	0.	1.00E+00	1.91E-01	1.60E+04	3.62E-02	1.60E+04	
5.82E+00	-6.31E+03	-4.13E+06	0.	1.00E+00	1.94E-01	1.60E+04	3.62E-02	1.60E+04	
5.92E+00	-5.98E+03	-4.17E+06	0.	1.00E+00	1.98E-01	1.60E+04	3.63E-02	1.60E+04	
6.02E+00	-5.65E+03	-4.19E+06	0.	1.00E+00	2.02E-01	1.60E+04	3.63E-02	1.60E+04	
6.12E+00	-5.31E+03	-4.21E+06	0.	1.00E+00	2.05E-01	1.60E+04	3.63E-02	1.60E+04	
6.23E+00	-4.97E+03	-4.22E+06	0.	1.00E+00	2.09E-01	1.60E+04	3.64E-02	1.60E+04	
6.33E+00	-4.63E+03	-4.22E+06	0.	1.00E+00	2.13E-01	1.61E+04	3.64E-02	1.61E+04	
6.43E+00	-4.29E+03	-4.22E+06	0.	1.00E+00	2.16E-01	1.61E+04	3.65E-02	1.61E+04	
6.53E+00	-3.95E+03	-4.20E+06	0.	1.00E+00	2.20E-01	1.61E+04	3.65E-02	1.61E+04	
6.63E+00	-3.62E+03	-4.18E+06	0.	1.00E+00	2.24E-01	1.61E+04	3.65E-02	1.61E+04	
6.73E+00	-3.28E+03	-4.15E+06	0.	1.00E+00	2.29E-01	1.61E+04	3.65E-02	1.61E+04	
6.83E+00	-2.95E+03	-4.12E+06	0.	1.00E+00	3.00E-01	1.61E+04	3.66E-02	1.61E+04	
6.93E+00	-2.62E+03	-4.08E+06	0.	1.00E+00	3.01E-01	1.61E+04	3.67E-02	1.62E+04	
7.03E+00	-2.29E+03	-4.03E+06	0.	1.00E+00	3.02E-01	1.62E+04	3.67E-02	1.62E+04	
7.13E+00	-1.97E+03	-3.98E+06	0.	1.00E+00	3.02E-01	1.62E+04	3.67E-02	1.62E+04	
7.23E+00	-1.65E+03	-3.93E+06	0.	1.00E+00	3.03E-01	1.62E+04	3.68E-02	1.62E+04	
7.33E+00	-1.34E+03	-3.87E+06	0.	1.00E+00	3.03E-01	1.62E+04	3.68E-02	1.62E+04	
7.43E+00	-1.03E+03	-3.80E+06	0.	1.00E+00	3.04E-01	1.62E+04	3.68E-02	1.62E+04	
7.53E+00	-7.30E+02	-3.74E+06	0.	1.00E+00	3.04E-01	1.62E+04	3.68E-02	1.62E+04	
7.63E+00	-4.33E+02	-3.67E+06	0.	1.00E+00	3.05E-01	1.62E+04	3.69E-02	1.63E+04	
7.73E+00	-1.41E+02	-3.59E+06	0.	1.00E+00	3.05E-01	1.62E+04	3.69E-02	1.63E+04	
7.83E+00	-1.44E+02	-3.52E+06	0.	1.00E+00	3.06E-01	1.62E+04	3.69E-02	1.63E+04	
7.93E+00	-4.23E+02	-3.44E+06	0.	1.00E+00	3.06E-01	1.62E+04	3.70E-02	1.63E+04	
8.03E+00	-6.96E+02	-3.36E+06	0.	1.00E+00	3.07E-01	1.62E+04	3.70E-02	1.63E+04	
8.13E+00	-9.63E+02	-3.27E+06	0.	1.00E+00	3.07E-01	1.62E+04	3.70E-02	1.63E+04	
8.23E+00	-1.22E+03	-3.19E+06	0.	1.00E+00	3.08E-01	1.62E+04	3.71E-02	1.63E+04	
8.33E+00	-1.47E+03	-3.10E+06	0.	1.00E+00	3.08E-01	1.62E+04	3.71E-02	1.63E+04	
8.43E+00	-1.72E+03	-3.01E+06	0.	1.00E+00	3.08E-01	1.62E+04	3.71E-02	1.64E+04	
8.53E+00	-1.96E+03	-2.92E+06	0.	1.00E+00	3.09E-01	1.64E+04	3.72E-02	1.64E+04	
8.64E+00	-2.19E+03	-2.83E+06	0.	1.00E+00	3.10E-01	1.64E+04	3.72E-02	1.64E+04	
8.74E+00	-2.41E+03	-2.74E+06	0.	1.00E+00	3.10E-01	1.64E+04	3.72E-02	1.64E+04	
8.84E+00	-2.63E+03	-2.65E+06	0.	1.00E+00	3.10E-01	1.64E+04	3.72E-02	1.64E+04	
8.94E+00	-2.84E+03	-2.55E+06	0.	1.00E+00	3.11E-01	1.64E+04	3.72E-02	1.64E+04	
9.04E+00	-3.04E+03	-2.46E+06	0.	1.00E+00	3.11E-01	1.64E+04	3.72E-02	1.64E+04	
9.14E+00	-3.23E+03	-2.37E+06	0.	1.00E+00	3.11E-01	1.64E+04	3.73E-02	1.64E+04	
9.24E+00	-3.42E+03	-2.27E+06	0.	1.00E+00	3.11E-01	1.64E+04	3.73E-02	1.64E+04	
9.34E+00	-3.60E+03	-2.18E+06	0.	1.00E+00	3.11E-01	1.64E+04	3.73E-02	1.64E+04	
9.44E+00	-3.77E+03	-2.08E+06	0.	1.00E+00	3.11E-01	1.64E+04	3.73E-02	1.64E+04	
9.54E+00	-3.93E+03	-1.99E+06	0.	1.00E+00	3.11E-01	1.64E+04	3.73E-02	1.64E+04	
9.64E+00	-4.09E+03	-1.89E+06	0.	1.00E+00	3.11E-01	1.64E+04	3.73E-02	1.64E+04	
9.74E+00	-4.24E+03	-1.80E+06	0.	1.00E+00	3.11E-01	1.64E+04	3.73E-02	1.64E+04	
9.84E+00	-4.38E+03	-1.71E+06	0.	1.00E+00	3.11E-01	1.64E+04	3.73E-02	1.64E+04	
9.94E+00	-4.51E+03	-1.61E+06	0.	1.00E+00	3.11E-01	1.64E+04	3.73E-02	1.64E+04	

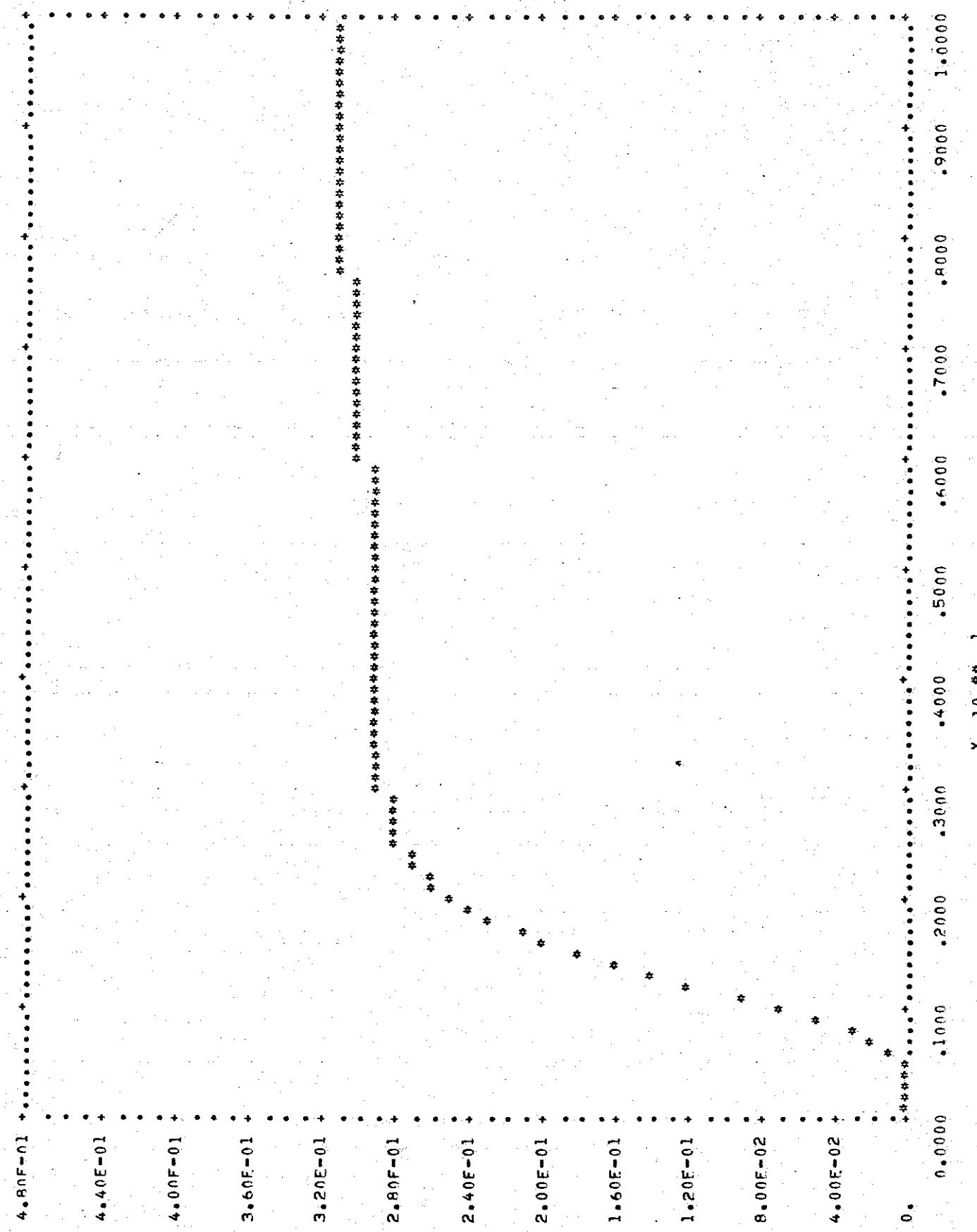
## CAPACITOR VOLTAGE VS TIME



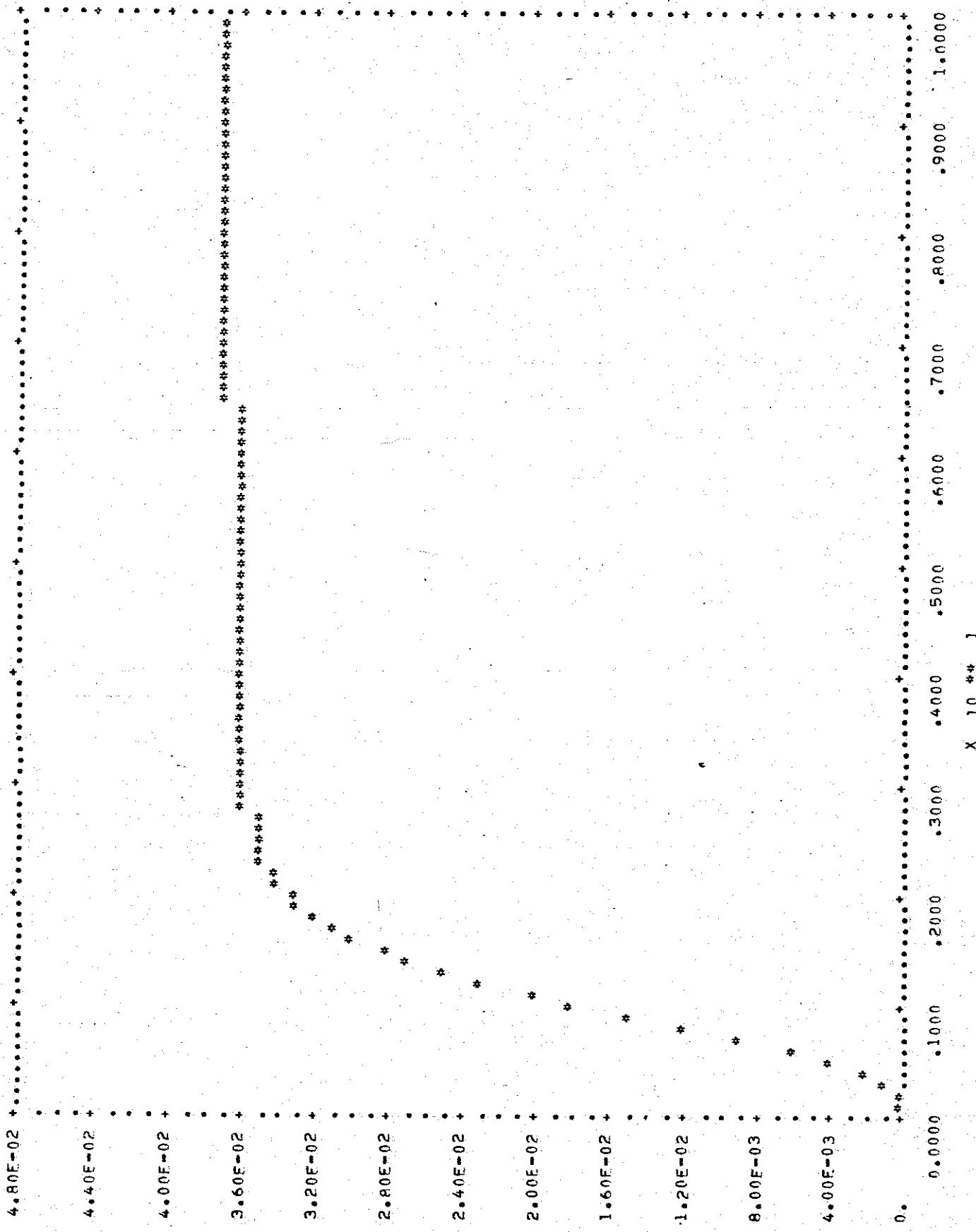
## FLYER CURRENT VS TIME



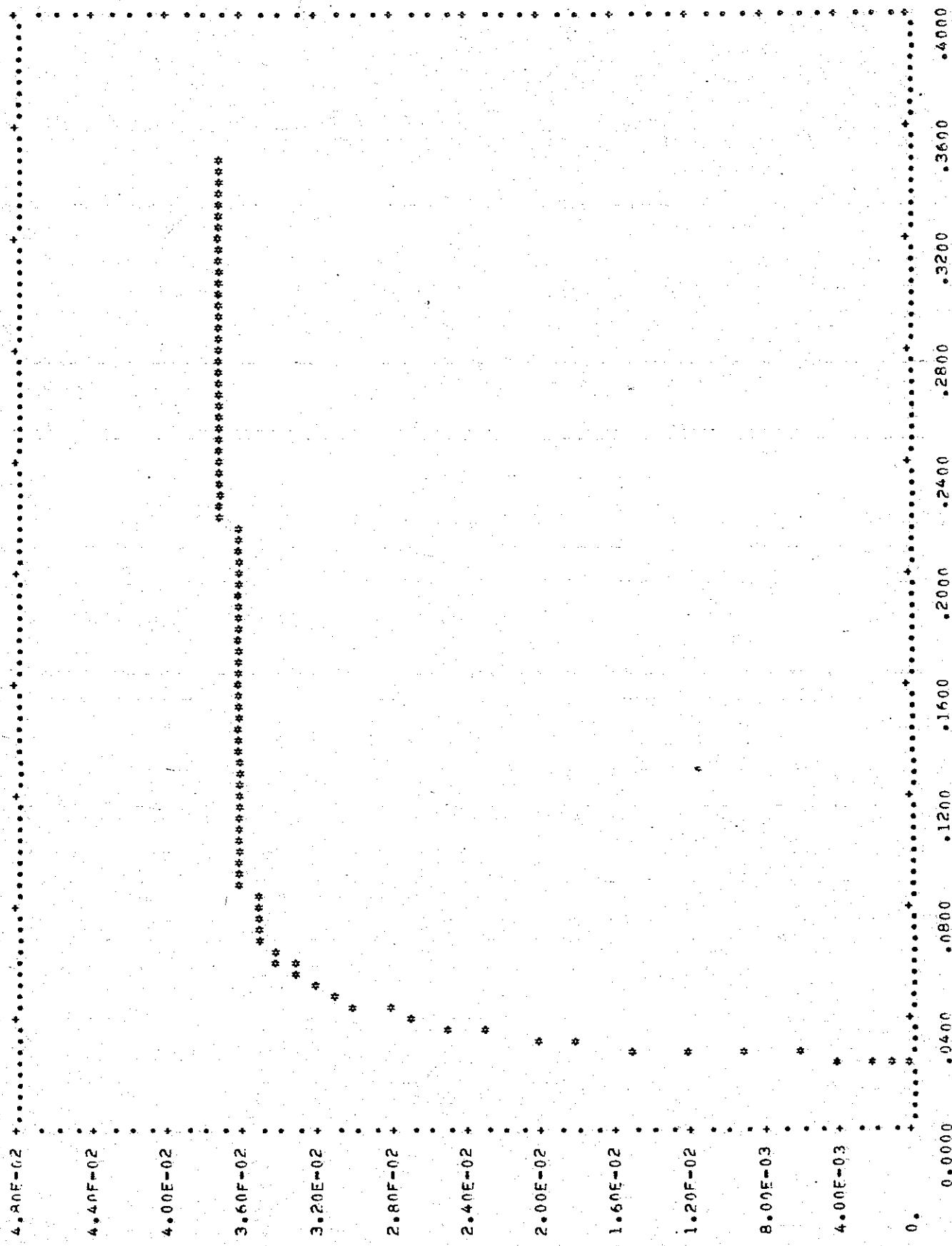
## EFFICIENCY VS TIME



## FLYER VELOCITY VS TIME



## FLYER VELOCITY VS DISTANCE



## DISTANCE vs TIME

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